


8. Find the values of the missing trig functions given $\sin \theta = -\frac{8}{17}$ and $\cos \theta = \frac{15}{17}$.

For questions 9- 15, find the exact value of each expression.

9. $\tan \frac{9\pi}{2}$

10. $\sec \frac{-11\pi}{4}$

11. $\sin \frac{-35\pi}{6}$

$\alpha = 30^\circ$ 

(12) $\cot \frac{19\pi}{6}$

$\cot\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{3}$

$\frac{1}{2} \cdot \frac{2}{\sqrt{3}} = \frac{\sqrt{3}}{3}$

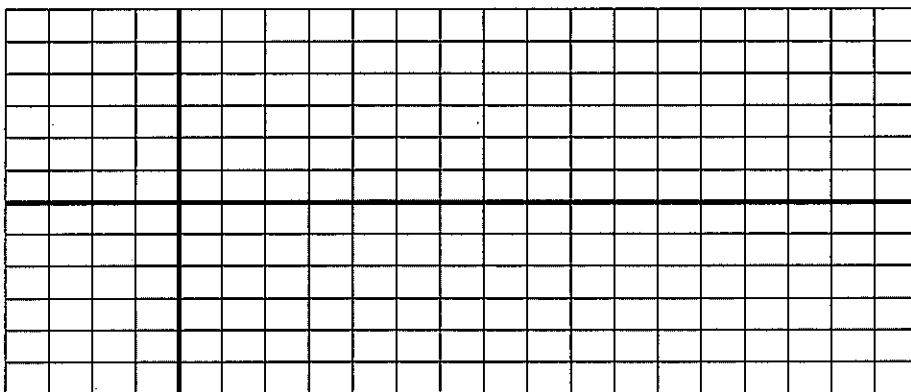
13. $\sec 510^\circ$

14. $\sin \frac{3\pi}{2} \tan \left(-\frac{8\pi}{3}\right) + \cos \left(-\frac{5\pi}{6}\right)$

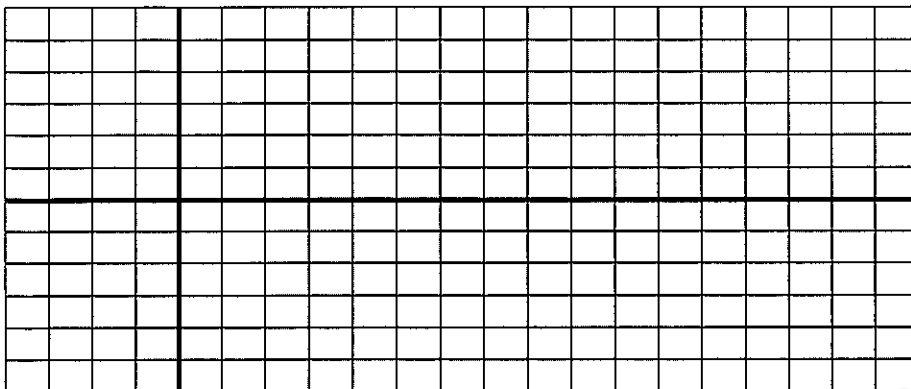
15. $\frac{\tan 150^\circ \csc 240^\circ}{\cos 135^\circ - \sin 300^\circ}$

For questions 16-19, graph one period of each function. Fully label your axes!! Use color for your final function!

16. $f(x) = 2 - 3 \sec 4(x - \pi)$



17. $f(x) = -1 + 4 \sin \frac{1}{2}(\theta + 45^\circ)$



$$22. \tan\left(x + \frac{\pi}{4}\right) + 1 = \sqrt{2} \cos x \sec\left(x + \frac{\pi}{4}\right)$$

$$23. (1 + \tan x) \tan 2x = \frac{2 \tan x}{1 - \tan x}$$

For questions 24-27, solve each equation in the indicated domain.

$$24. 2 \cot^2 x + 2 \cot x = 0, \text{ Domain: } (-\infty, \infty) \quad \frac{\pi - \frac{\pi}{4} = \frac{3\pi}{4}}{\frac{3\pi}{4}} \quad 25. 4 \csc^2 \theta + 4 \csc \theta + 1 = 0, \text{ Domain: } [0^\circ, 360^\circ)$$

$$2 \cot x (\cot x + 1) = 0$$

$$2 \cot x = 0 \quad \cot x = -1$$

$$\frac{\cos}{\sin} = 0 \quad \frac{\pi}{2} + 2\pi n \quad \frac{3\pi}{4} + 2\pi n$$

$$\frac{3\pi}{2} + 2\pi n \quad \frac{7\pi}{4} + 2\pi n$$

$$26. 1 - \cos \theta = -\sin \theta, \text{ Domain: } [-180^\circ, 180^\circ)$$

$$27. \frac{\tan 10\theta + \tan 50^\circ}{1 - \tan 10\theta \tan 50^\circ} = \frac{\sqrt{3}}{3}, \text{ Domain: } (0^\circ, 90^\circ)$$

- a. $x = -3$
 b. $y = -2$

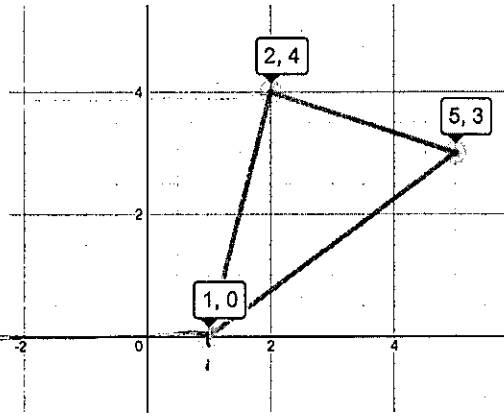
$$V_F = \frac{\pi}{3} (5^2 + 40 + 8^2) = 43\pi$$

$$V_F = \frac{\pi}{3} (3) (4^2 + 32 + 8^2) = 112\pi$$

$$V_F = \frac{\pi}{3} (4) (4^2 + 20 + 5^2) = \frac{244\pi}{3}$$

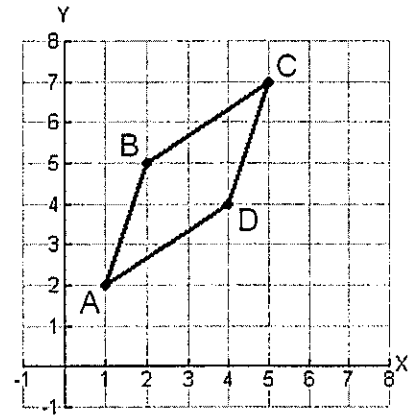
$$156\pi - \frac{244\pi}{3}$$

$$\frac{465}{3} - \frac{244\pi}{3} = \frac{221\pi}{3}$$



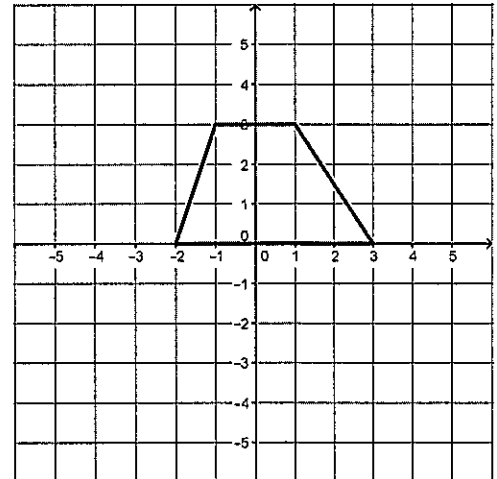
48. Find the volume of the solid formed when the triangle is rotated about

- a. $x = -1$.
 b. $y = 5$.



49. Find the volume of the solid formed when the trapezoid is rotated about

- a. $y = 4$
 b. $x = -3$



50. Find the volume of a hollow sphere, where the outer diameter is 15cm and the length of the inner diameter is 7cm.

51. Find the volume of the frustum with $r_1 = x + 3$, $r_2 = 2x - 1$, and $h = 4x$.

52. Is $3 - i$ a zero to the function $g(x) = x^3 - 10x^2 + 34x - 40$?

$$\begin{aligned}
 (3-i)^2 &= 9 - 6i - 1 = \underline{8-6i} \\
 (8-6i)(3-i) &= 24 - 18i - 8i - 6 = \underline{18-26i} \\
 (18-26i) - 10(8-6i) + 34(3-i) - 40 &= 18 - 26i - 80 + 60i + 102 - 34i - 40 = 0 \quad \boxed{\text{Yes!}}
 \end{aligned}$$

53. At 1:00pm (13:00) high tide was at 4 feet, at 8:00 pm (20:00) low tide was -1 feet. Find the period of the trigonometric function that would model the tides.

54. Simplify

$$\frac{3 + \frac{x}{2-x}}{\frac{1}{x} - 4}$$

55. Factor the following polynomial: $125x^3 - 8y^6$

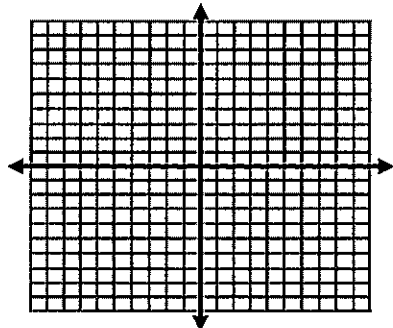
56. Expand the binomial: $(5y - x^3)^5$

57. Divide using long division or unboxing method:

$$\frac{2x^3 - 4x + 512x^3 - 11x^2 + 22x - 15}{x^2 - 4x + 5}$$

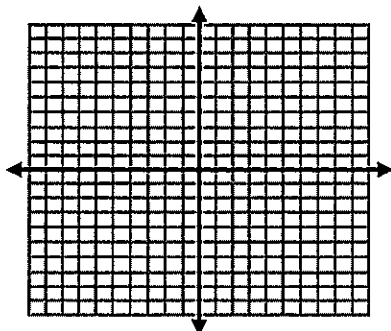
Graph the function and label the following information. Horizontal Asymptotes can include slant asymptotes.

44. $y = \frac{x^2 + 4x - 5}{x + 1}$



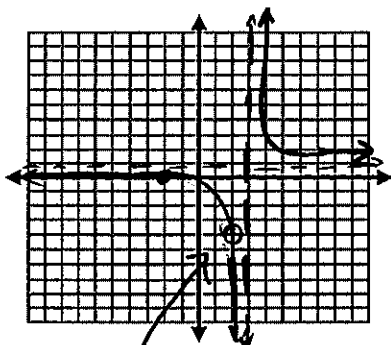
| | |
|------------------------|--|
| Zeros: | |
| Vertical Asymptotes: | |
| Horizontal Asymptotes: | |
| Holes: | |
| Y-Intercept(s): | |
| Domain: | |
| range | |

45. $y = \frac{x^2 + 5x + 6}{x^2 - 9}$



| | |
|------------------------|--|
| Zeros: | |
| Vertical Asymptotes: | |
| Horizontal Asymptotes: | |
| Holes: | |
| Y-Intercept(s): | |
| Domain: | |
| range | |

46. $y = \frac{(x+2)(x-2)}{3x^2 - 15x + 18}$
 $\frac{3(x^2 - 5x + 6)}{(x-3)(x+2)}$



HOLE!

| | |
|------------------------|---|
| Zeros: | $x = -2$ |
| Vertical Asymptotes: | $x = 3$ |
| Horizontal Asymptotes: | $y = \frac{1}{3}$ |
| Holes: | $x = 2$ |
| Y-Intercept(s): | $y = -\frac{2}{9}$ |
| Domain: | $(-\infty, 2) \cup (2, 3) \cup (3, \infty)$ |
| range | |

47. Find the volume of the solid formed when the rectangle shown is rotated about
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