

For questions 1-2, perform the given operation. Leave your answers as factored as possible.

1.  $\frac{6x^2 + 5x - 4}{2x^2 - 17x + 8} \cdot \frac{x^2 - 4x - 32}{12x^2 - 5x - 2}$

$\frac{(3x+4)(2x-1) \cdot (x-8)(x+4)}{(2x-1)(x-8) (4x+1)(3x-2)}$

$\frac{(3x+4)(x+4)}{(4x+1)(3x-2)}$

2.  $\frac{3}{x+2} + \frac{4}{x^2-4} - \frac{1}{x^2-x-2}$

$\frac{3(x-2)(x+1) + 4(x+1) - (x+2)}{(x-2)(x+2)(x+1) (x-2)(x-2)(x+1)}$

$\frac{3x^2 - 3x - 6 + 4x + 4 - x - 2}{(x-2)(x+2)(x+1)} = \frac{3x^2 - 4}{(x-2)(x+2)(x+1)}$

For questions 3-5, find all the zeros (real & imaginary) of each function.

3.  $f(x) = 2x^3 - 3x^2 - 11x + 6$

4.  $f(x) = x^4 - 2x^3 - 5x^2 + 8x + 4$

$\frac{4}{1} = \frac{1, 2, 4}{1} = \pm 1, \pm 2, \pm 4$

$\frac{6}{2} = \frac{1, 2, 3, 6}{1, 2} = \pm \frac{1}{2}, \pm 1, \pm 2, \pm 3, \pm \frac{3}{2}, \pm 6$

$f(2) = 16 - 16 - 20 + 16 + 4 = 0 \checkmark$

$f(-2) = -16 - 12 + 22 + 6 = 0 \checkmark$

$x+2 \overline{) 2x^3 - 3x^2 - 11x + 6}$   
 $\underline{-(2x^3 + 4x^2)}$   
 $-7x^2 - 11x + 6$   
 $\underline{-(-7x^2 - 14x)}$   
 $3x + 6$   
 $\underline{-(3x + 6)}$   
 $0$

$(x+2)(2x^2 - 7x + 3)$   
 $(x+2)(2x-1)(x-3)$   
 $x = -2, x = \frac{1}{2}, x = 3$

$x-2 \overline{) x^4 - 2x^3 - 5x^2 + 8x + 4}$   
 $\underline{-(x^4 - 2x^3)}$   
 $-5x^2 + 8x + 4$   
 $\underline{-(-5x^2 + 10x)}$   
 $-2x + 4$   
 $\underline{-(-2x + 4)}$   
 $0$

$f(x) = x^3 - 5x - 2$   $\frac{2}{1} = \frac{1, 2}{1} = \pm 1, \pm 2$   
 $f(-2) = -8 + 10 - 2 = 0 \checkmark$

5.  $f(x) = x^3 + 7x^2 + x + 7$

$x^2(x+7) + 1(x+7)$

$(x^2 + 1)(x + 7)$

$x^2 + 1 = 0$

$x^2 = -1$

$x = \pm i$

$x = -7$

$x+2 \overline{) x^3 - 5x - 2}$   
 $\underline{-(x^3 + 2x^2)}$   
 $-2x^2 - 5x - 2$   
 $\underline{-(-2x^2 - 4x)}$   
 $-x - 2$   
 $\underline{-(-x - 2)}$   
 $0$

$(x+2)(x-2)(x^2 - 2x - 1)$   
 $x = -2, x = 2$

$x = \frac{2 \pm \sqrt{4 - 4(1)(-1)}}{2(1)}$

$x = \frac{2 \pm 2\sqrt{2}}{2}$

$x = 1 \pm \sqrt{2}$

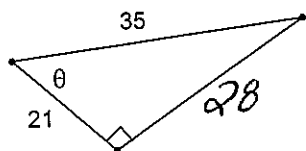
6. Write the polynomial function of least degree & with integer coefficients if the zeros occur at 6 and  $-5 + 2i$ .

$(x-6)(x+5-2i)(x+5+2i)$

$(x-6)(x^2 + 10x + 29)$

$x^3 + 4x^2 - 31x - 174$

7. Find the value of each of the six trig functions of  $\theta$ .



$\sin \theta = \frac{28}{35} = \frac{4}{5}$

$\cos \theta = \frac{21}{35} = \frac{3}{5}$

$\tan \theta = \frac{28}{21} = \frac{4}{3}$

8. Find the values of the missing trig functions given  $\sin \theta = -\frac{8}{17}$  and  $\cos \theta = \frac{15}{17}$ .

$$\csc \theta = -\frac{17}{8}$$

$$\sec \theta = \frac{17}{15}$$

$$\cot \theta = -\frac{15}{8}$$

$$\tan \theta = \frac{-\frac{8}{17}}{\frac{15}{17}} = -\frac{8}{15}$$

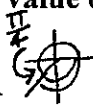
For questions 9-15, find the exact value of each expression.

9.  $\tan \frac{9\pi}{2}$



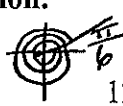
undefined

10.  $\sec \frac{-11\pi}{4}$



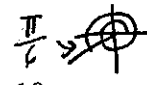
$$\sec \frac{\pi}{4} = \sqrt{2}$$

11.  $\sin \frac{-35\pi}{6}$



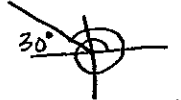
$$\sin \frac{\pi}{6} = \frac{1}{2}$$

12.  $\cot \frac{19\pi}{6}$



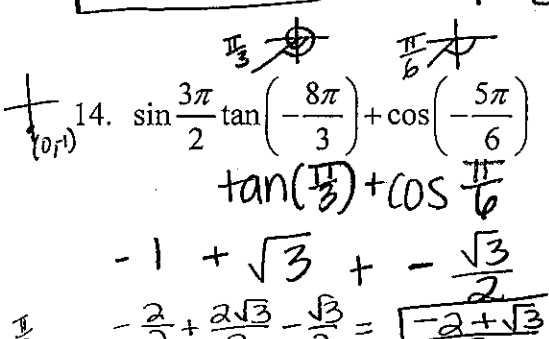
$$\cot \frac{5\pi}{6} = -\frac{\sqrt{3}}{1} = -\sqrt{3}$$

13.  $\sec 510^\circ$



$$\sec(150^\circ) = -\frac{2}{\sqrt{3}}$$

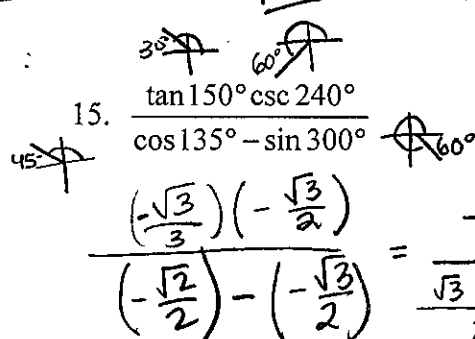
14.  $\sin \frac{3\pi}{2} \tan \left(-\frac{8\pi}{3}\right) + \cos \left(-\frac{5\pi}{6}\right)$



$$\tan \left(-\frac{2\pi}{3}\right) + \cos \frac{\pi}{6}$$

$$-1 + \sqrt{3} + \frac{1}{2} = \frac{-2 + 2\sqrt{3} + 1}{2} = \frac{-1 + 2\sqrt{3}}{2}$$

15.  $\frac{\tan 150^\circ \csc 240^\circ}{\cos 135^\circ - \sin 300^\circ}$

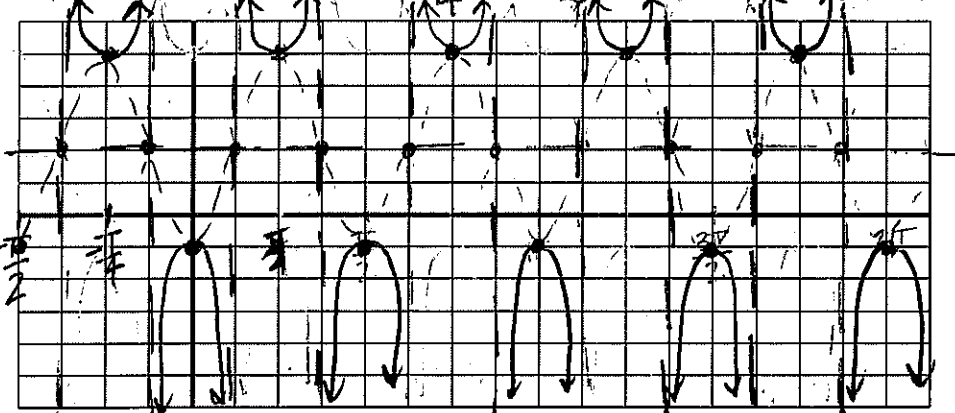


$$\frac{\left(-\frac{\sqrt{3}}{2}\right)\left(-\frac{1}{2}\right)}{\left(-\frac{\sqrt{2}}{2}\right) - \left(-\frac{1}{2}\right)} = \frac{\frac{3}{4}}{\frac{-\sqrt{2} + 1}{2}} = \frac{3}{2(-\sqrt{2} + 1)} = \frac{3(2)}{2(2 - \sqrt{2})} = \frac{3}{2 - \sqrt{2}}$$

For questions 16-19, graph one period of each function. Fully label your axes!! Use color for your final function!

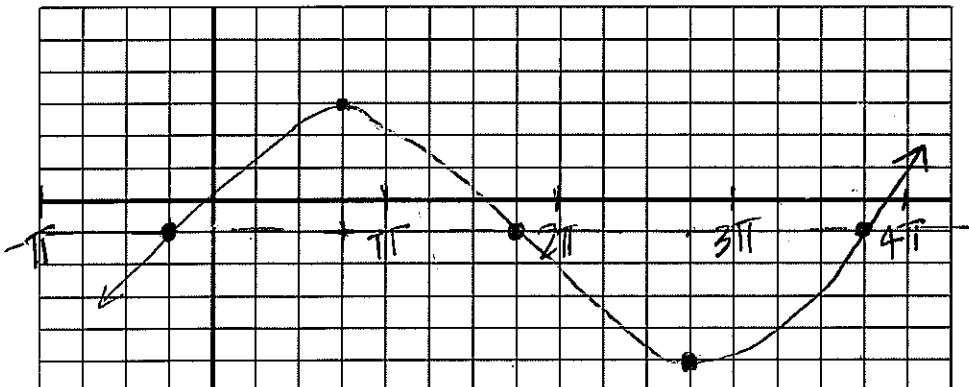
16.  $f(x) = 2 - 3 \sec 4(x - \pi)$

Period  $\frac{2\pi}{4} = \frac{\pi}{2}$ . Phase shift  $\pi$

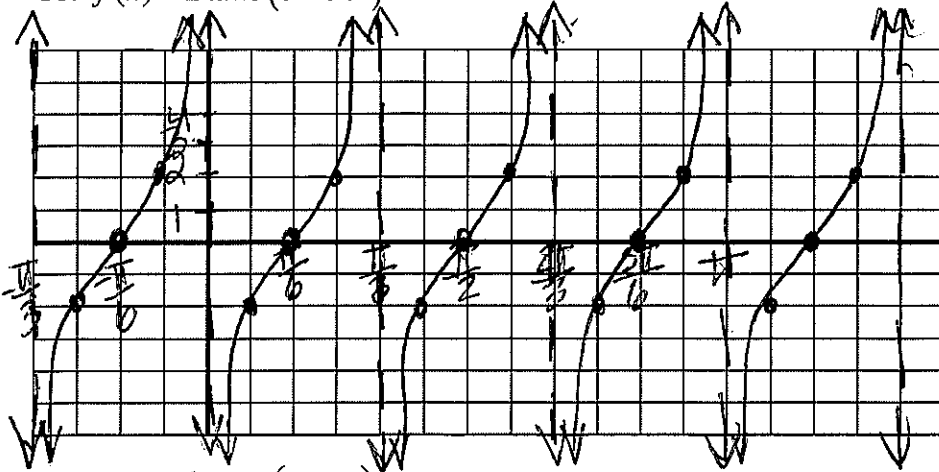


17.  $f(x) = -1 + 4 \sin \frac{1}{2}(\theta + 45^\circ)$

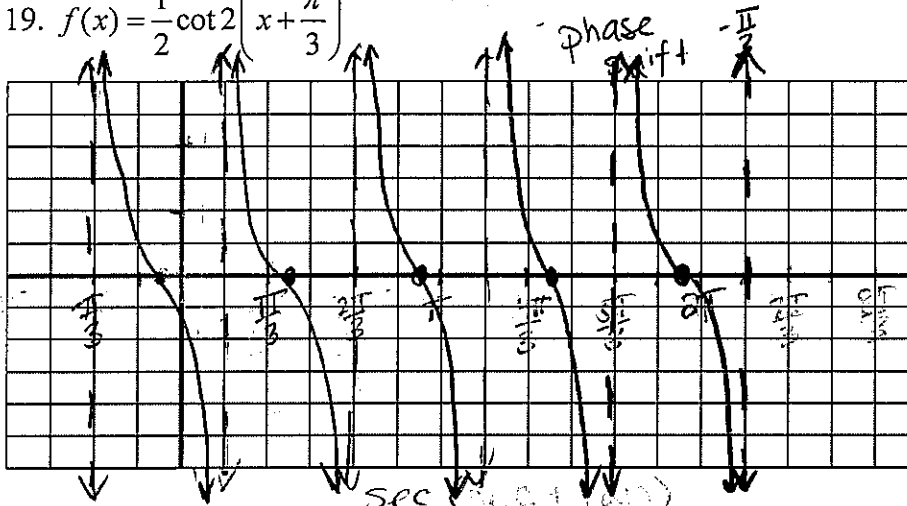
$\frac{2\pi}{1/2} = 4\pi$



18.  $f(x) = 2 \tan 3(\theta - 30^\circ)$



19.  $f(x) = \frac{1}{2} \cot 2\left(x + \frac{\pi}{3}\right)$

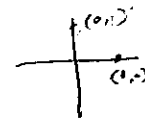


$$2\left(x + \frac{\pi}{3}\right) = 0 \quad 2\left(x + \frac{\pi}{3}\right) = \pi$$

$$x = -\frac{\pi}{3} \quad x = \frac{\pi}{2} - \frac{\pi}{3}$$

$$x = \frac{\pi}{6}$$

$$\frac{2\pi}{2} = \frac{\pi}{1}$$



$$\cot = \frac{\cos}{\sin}$$

For questions 20-23, prove each identity.

20.  $\frac{1}{1 - \sin x} = \sec^2 x + \sec x \tan x$

$$= 1 + \tan^2 x + \left(\frac{1}{\cos x}\right) \left(\frac{\sin x}{\cos x}\right)$$

$$= \frac{\cos^2}{\cos^2} + \frac{\sin^2}{\cos^2} + \frac{\sin x}{\cos^2}$$

$$= \frac{\cos^2 + \sin^2 + \sin x}{\cos^2}$$

$$= \frac{1 + \sin x}{1 - \sin^2 x}$$

$$= \frac{1 + \sin x}{(1 + \sin x)(1 - \sin x)}$$

$$= \frac{1}{1 - \sin x}$$

$\sin^2 + \cos^2 = 1$   
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21.  $\frac{\sec^3 x - \cos^3 x}{\sec x - \cos x} = \sec^2 x + 1 + \cos^2 x$

$$\frac{(\sec - \cos)(\sec^2 + \cos \sec + \cos^2)}{(\sec - \cos)}$$

$$\sec^2 + \cos \sec + \cos^2$$

$$\sec^2 + \cos \frac{1}{\cos} + \cos^2$$

$$\sec^2 + 1 + \cos^2 x = \checkmark$$

$$1 + \tan^2 = \sec^2$$

$$1 + \cot^2 = \csc^2$$

Need to work both sides

$$22. \tan\left(x + \frac{\pi}{4}\right) + 1 = \sqrt{2} \cos x \sec\left(x + \frac{\pi}{4}\right)$$

$$\frac{\tan x + \tan \frac{\pi}{4}}{1 - \tan x \tan \frac{\pi}{4}} + 1 = \sqrt{2} \cos x \frac{1}{\cos\left(x + \frac{\pi}{4}\right)}$$

$$\frac{\tan x + 1}{1 - \tan x} + \frac{1 - \tan x}{1 - \tan x} = \frac{2 \cos x}{\cos x - \sin x}$$

$$\frac{2}{1 - \tan x} = \frac{2 \cos x}{\cos x - \sin x}$$

$$\sqrt{2} \cos x \frac{1}{\cos x \cos \frac{\pi}{4} - \sin x \sin \frac{\pi}{4}}$$

$$\sqrt{2} \cos x \left( \frac{1}{2(\cos x - \sin x)} \right)$$

$$\frac{2 \cos x}{\cos x - \sin x}$$

$$23. (1 + \tan x) \tan 2x = \frac{2 \tan x}{1 - \tan x}$$

$$(1 + \tan x) \frac{2 \tan x}{1 - \tan^2 x} + \tan x \frac{2 \tan x}{(1 + \tan x)(1 - \tan x)}$$

$$\frac{2 \tan x}{1 - \tan x} = \checkmark$$

For questions 24-27, solve each equation in the indicated domain.

$$24. 2 \cot^2 x + 2 \cot x = 0, \text{ Domain: } (-\infty, \infty)$$

$$2 \cot x (\cot x + 1) = 0$$

$$2 \cot x = 0 \quad \cot x = -1$$

$$\cot x = 0$$

$x = \pi + 2\pi n$	$x = \frac{3\pi}{4} + 2\pi n$
$x = 0 + 2\pi n$	$x = \frac{7\pi}{4} + 2\pi n$

$$25. 4 \csc^2 \theta + 4 \csc \theta + 1 = 0, \text{ Domain: } [0^\circ, 360^\circ)$$

$$(2 \csc \theta + 1)(2 \csc \theta + 1) = 0$$

$$2 \csc \theta + 1 = 0$$

$$\csc \theta = -\frac{1}{2}$$

undefined

$$26. (1 - \cos \theta)^2 = (-\sin \theta)^2, \text{ Domain: } [-180^\circ, 180^\circ)$$

$$1 - 2 \cos \theta + \cos^2 \theta = \sin^2 \theta$$

$$1 - 2 \cos \theta + \cos^2 \theta = 1 - \cos^2 \theta$$

$$-2 \cos \theta + 2 \cos^2 \theta = 0$$

$$2 \cos \theta (-1 + \cos \theta) = 0$$

$$2 \cos \theta = 0 \quad -1 + \cos \theta = 0$$

$$\cos \theta = 0 \quad \cos \theta = 1$$

$$\theta = 90^\circ, -90^\circ \quad \theta = 0^\circ$$

$$27. \frac{\tan 10\theta + \tan 50^\circ}{1 - \tan 10\theta \tan 50^\circ} = \frac{\sqrt{3}}{3}, \text{ Domain: } (0^\circ, 90^\circ)$$

$$\tan(10\theta + 50^\circ) = \frac{\sqrt{3}}{3}$$

$$10\theta + 50^\circ = 30^\circ$$

$$10\theta = -20^\circ$$

$$\theta = -2^\circ$$

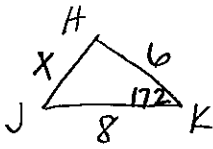
$$10\theta + 50^\circ = 210^\circ$$

$$10\theta = 160^\circ$$

$$\theta = 16^\circ$$

For triangle questions 28-31, find the specified side or angle. Round your answers to 2 decimal places.

28. In  $\triangle HJK$ ,  $h = 8$ ,  $j = 6$ ,  $m\angle K = 172^\circ$ , find  $k$ .



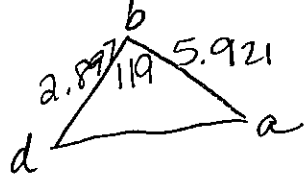
$$k^2 = 6^2 + 8^2 - 2(6)(8)\cos 172$$

$$k^2 = 100 + 64 - 96 \cos 172$$

$$k = 13.96659$$

$$k = 13.97$$

29. In  $\triangle BAD$ ,  $a = 2.897$ ,  $d = 5.921$ ,  $m\angle B = 119^\circ$ , find  $b$ .

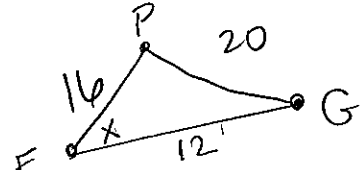


$$b^2 = 2.897^2 + 5.921^2 - 2(2.897)(5.921)\cos(119)$$

$$b^2 = 8.818 + 35.056 - 34.21 \cos(119)$$

$$\sqrt{b^2} = \sqrt{5.45001167} \quad b = 5.04$$

30. In  $\triangle PEG$ ,  $p = 12$ ,  $e = 20$ ,  $g = 16$ , find  $m\angle E$ .

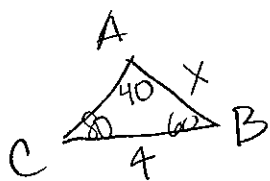


$$20^2 = 12^2 + 16^2 - 2(12)(16)\cos x$$

$$400 = 400 - 384 \cos x$$

$$0 = \cos x \quad x = 90^\circ$$

31. In  $\triangle ABC$ ,  $m\angle A = 40^\circ$ ,  $m\angle B = 60^\circ$ ,  $a = 4$ , find  $c$ .



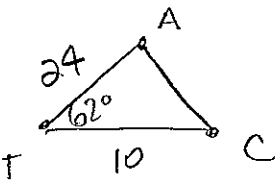
$$\frac{\sin 80}{x} = \frac{\sin 40}{4}$$

$$\frac{4 \sin 80}{\sin 40} = x$$

$$x = 6.13$$

For questions 32-33, find the area of each triangle. Round your answers to 2 decimal places.

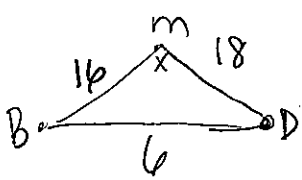
32.  $c = 24$  meters,  $a = 10$  meters,  $T = 62^\circ$



$$\frac{1}{2}(24)(10)\sin 62$$

$$105.95$$

33.  $m = 6$  feet,  $d = 16$  feet, and  $b = 18$  feet.



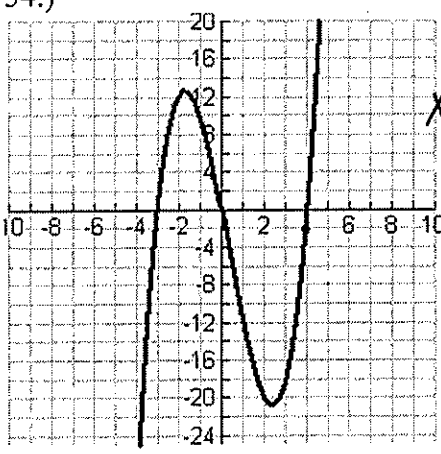
$$6^2 = 16^2 + 18^2 - 2(16)(18)\cos x$$

$$36 = 580 - 576 \cos x$$

$$x = 19.19$$

For #34-35, write the equation of the polynomial function graphed with lowest degree possible and leading coefficient of 1.

34.)

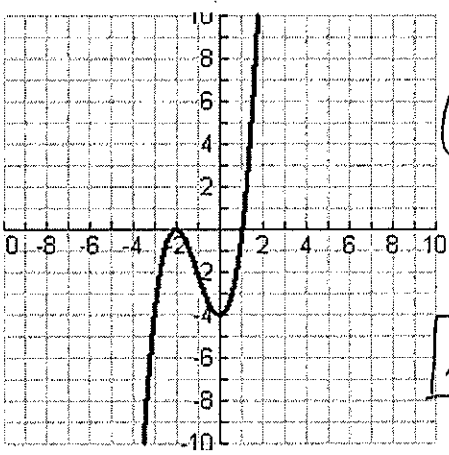


$$x(x+3)(x-4)$$

$$x(x^2 - x - 12)$$

$$x^3 - x^2 - 12x$$

35.)



$$(x+2)(x-1)$$

$$(x^2 + 4x + 4)(x-1)$$

$$x^3 + 4x^2 + 4x - x^2 - 4x - 4$$

$$x^3 + 3x^2 - 4$$

For questions 36-40, find all the zeros of the polynomial function.

36.  $f(x) = 2x^3 - 2x^2 + 16x + 120$

$$2(x^3 - x^2 + 8x + 60)$$

$$f(-3) = -27 - 9 - 24 + 60$$

$$-60 + 60 = 0$$

$$2x^2 - 8x + 40 = 2(x^2 - 4x + 20)$$

$$x+3 \overline{) 2x^3 - 2x^2 + 16x + 120}$$

$$-2x^3 + 6x^2$$

$$-8x^2 + 16x$$

$$-(-8x^2 - 24x)$$

$$40x + 120$$

$$40x + 120$$

$$0$$

39.  $f(x) = x^3 + 12x^2 + 21x + 10$

$$f(-1) = -1 + 12 - 21 + 10$$

$$x+1 \overline{) x^3 + 12x^2 + 21x + 10}$$

$$11x^2 + 21x$$

$$+11x^2 + 11x$$

$$10x + 10$$

$$10x + 10$$

$$0$$

$$(x+1)(x+10)(x+1)$$

$$x = -1, -10$$

37.  $f(x) = x^4 - 3x^3 - 2x^2 - 6x - 8$

$$f(-1) = 0$$

$$x+1 \overline{) x^4 - 3x^3 - 2x^2 - 6x - 8}$$

$$-(x^4 + x^3)$$

$$-4x^3 - 2x^2$$

$$-(-4x^3 - 4x^2)$$

$$2x^2 - 6x$$

$$-(2x^2 + 2x)$$

$$-8x - 8$$

$$-8x - 8$$

$$0$$

$$(x-2)^2 = -20 + 4$$

$$(x-2)^2 = -16$$

$$x-2 = \pm 4i$$

$$x = 2 \pm 4i$$

$$x = -3$$

$$x = -1, 4, \pm i\sqrt{2}$$

40.  $f(x) = x^4 + x^3 - x^2 + x - 2$

$$f(-2) = 0 \quad f(1) = 0$$

$$(x+2)(x-1) = x^2 - x - 2$$

$$x^2 - x - 2 \overline{) x^4 + x^3 - x^2 + x - 2}$$

$$-(x^4 - x^3 - 2x^2)$$

$$x^2 + x - 2$$

$$x^2 - x - 2$$

$$0$$

$$(x+2)(x-1)(x^2+1)$$

$$x = -2, x = 1, x = \pm i$$

38.  $f(x) = 216x^3 + 64$

$$8(27x^3 + 8)$$

$$8(3x+2)(9x^2 - 6x + 4)$$

$$x = -\frac{2}{3} \quad x = \frac{6 \pm \sqrt{36 - 4(9)(4)}}{2(9)}$$

$$= \frac{6 \pm \sqrt{-108}}{18}$$

$$= \frac{6 \pm i6\sqrt{3}}{18}$$

$$= \frac{1 \pm i\sqrt{3}}{3}$$

Write a rational function with the given characteristics.

41.

There are no zeros, a hole exists at  $x = -3/2$ , vertical asymptote is at  $x = 1$ , and horizontal asymptote is at  $y = 0$ .

$$f(x) = \frac{(2x+3)}{(2x+3)(x-1)}$$

42. There is a zero at 6, a hole exists at  $x = -3$ , no vertical asymptotes, and horizontal asymptote at  $y = x - 6$ .

$$f(x) = \frac{(x-6)(x+3)}{(x+3)}$$

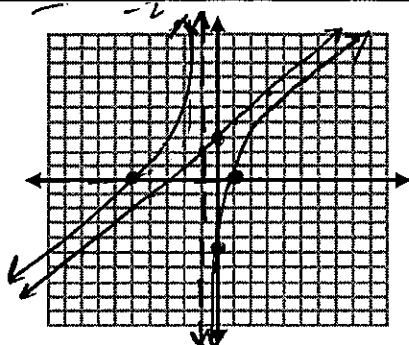
43. The zeros are at -1 and 3 and the vertical asymptote is at  $x = 0$ .

$$f(x) = \frac{(x+1)(x-3)}{x}$$

$$\begin{array}{r}
 x+3 \\
 x+1 \overline{) x^2+4x-5} \\
 \underline{x^2+x} \phantom{-5} \\
 3x-5 \\
 \underline{3x-3} \\
 -2
 \end{array}$$

Graph the function and label the following information. Horizontal Asymptotes can include slant asymptotes.

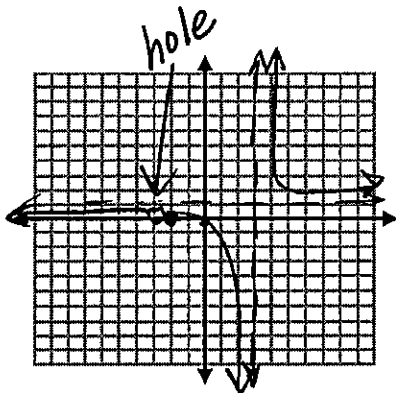
44.  $y = \frac{(x+5)(x-1)}{x+1}$



Zeros:	$x = -5, x = 1$
Vertical Asymptotes:	$x = -1$
Horizontal Asymptotes:	none
Holes:	none
Y-Intercept(s):	$(0, -5)$
Domain:	$(-\infty, -1) \cup (-1, \infty)$
range	$(-\infty, \infty)$

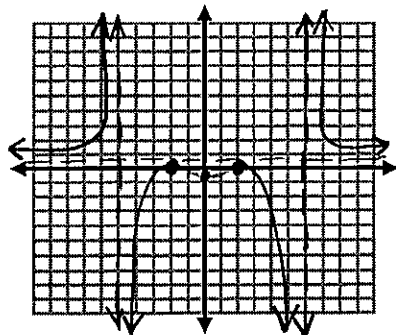
slant asymptote  $y = x + 3$

45.  $y = \frac{(x+3)(x+2)}{x^2-9}$   
 $\frac{(x+3)(x+2)}{(x+3)(x-3)}$



Zeros:	$x = -2$
Vertical Asymptotes:	$x = 3$
Horizontal Asymptotes:	$y = 1$
Holes:	$x = -3$
Y-Intercept(s):	$(0, -\frac{2}{3})$
Domain:	$(-\infty, 3) \cup (3, \infty)$
range	$(-\infty, \infty)$

46.  $y = \frac{(x+2)(x-2)}{3x^2-15x+18}$   
 $\frac{3(x^2-5x+6)}{3(x-6)(x+5)}$



Zeros:	$x = -2, x = 2$
Vertical Asymptotes:	$x = 6, x = -5$
Horizontal Asymptotes:	$y = \frac{1}{3}$
Holes:	none
Y-Intercept(s):	$(0, -\frac{2}{9})$
Domain:	$(-\infty, -5) \cup (-5, 6) \cup (6, \infty)$
range	$(-\infty, \infty)$

47. Find the volume of the solid formed when the rectangle shown is rotated about

# Volume of rectangle rotated about

a.  $x = -3$   $V_F + V_F - V_F$

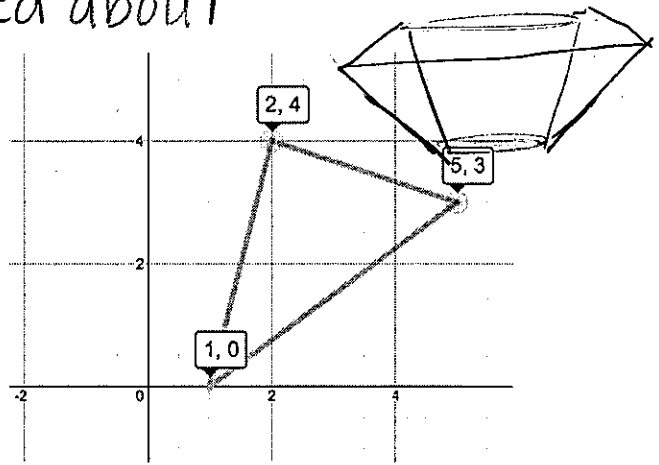
$$V_F = \frac{\pi}{3}(6^2 + 48 + 8^2) = \frac{148\pi}{3}$$

b.  $y = -2$

$$V_F = \frac{\pi}{3}(3)(4^2 + 32 + 8^2) = 122\pi$$

$$V_F = \frac{\pi}{3}(4)(4^2 + 20 + 5^2) = \frac{244\pi}{3}$$

$90\pi$



48. Find the volume of the solid formed when the triangle is rotated about

$$V_F + V_F - V_F - V_F \quad 91\pi - 19\pi = 72\pi$$

a.  $x = -1$

$$V_F = \frac{\pi}{3}(2)(2^2 + 5(2) + 5^2) = \frac{2\pi}{3}(39) = 26\pi$$

$$V_F = \frac{\pi}{3}(4)(2^2 + 6 + 3^2) = 19\pi$$

$$V_F = \frac{\pi}{3}(3)(5^2 + 30 + 36) = \pi(91) = 91\pi$$

$$V_F = \frac{\pi}{3}(2)(2^2 + 10 + 15) = 26\pi$$

b.  $y = 5$

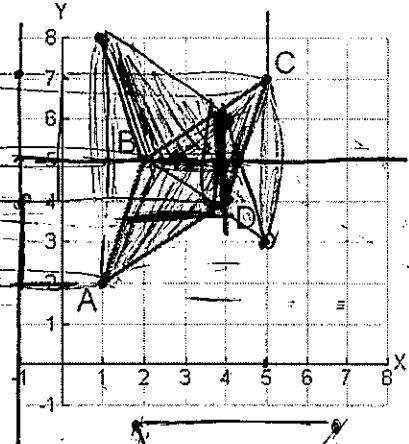
$$V_{F_1} + V_{C_1} + V_{F_2} - V_{C_2} \quad (13\pi - 3\pi) + \left(\frac{7\pi}{3} - \frac{4\pi}{3}\right) = 10\pi + \pi = 11\pi$$

$$V_{F_1} = \frac{\pi}{3}(3)(3^2 + 3 \cdot 1 + 1^2) = 13\pi$$

$$V_{F_2} = \frac{\pi}{3}(2^2 + 2 + 1) = \frac{7\pi}{3}$$

$$V_{C_1} = \frac{1}{3}(\pi 9) = 3\pi$$

$$V_{C_2} = \frac{1}{3}(\pi 4) = \frac{4\pi}{3}$$



49. Find the volume of the solid formed when the trapezoid is rotated about

a.  $y = 4$   $V_C - V_F - V_F = \pi(4)^2(5) - \frac{1}{3}\pi(1)(4^2 + 4 + 12)$

$$- \frac{1}{3}\pi(2)(4^2 + 4 + 12)$$

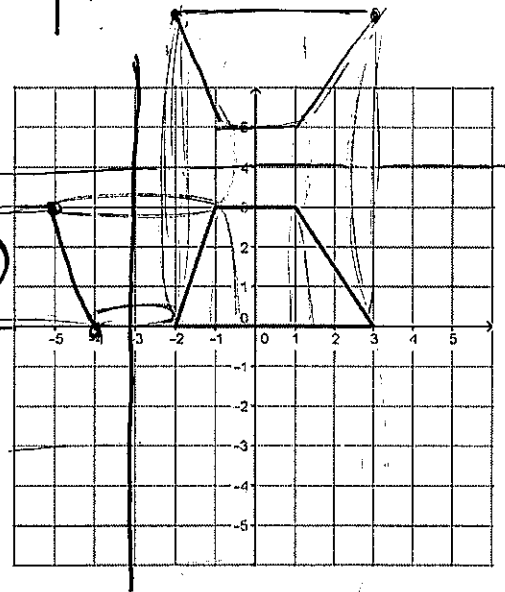
b.  $x = -3$

$$= 80\pi - 7\pi - 14\pi = 59\pi$$

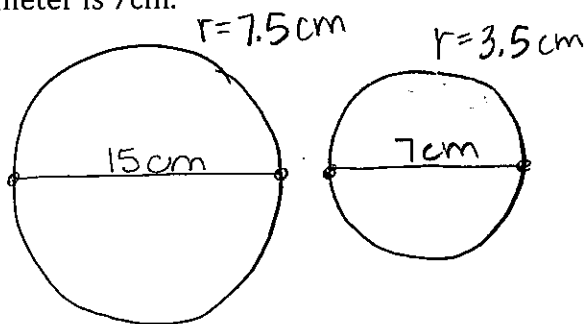
$$V_F - V_F$$

$$= \frac{1}{3}\pi(3)(6^2 + 24 + 4^2) - \frac{1}{3}\pi(3)(2^2 + 2 + 1)$$

$69\pi$



50. Find the volume of a hollow sphere, where the outer diameter is 15cm and the length of the inner diameter is 7cm.



$$\frac{4}{3}\pi\left(\frac{15}{2}\right)^3$$

$$\frac{4}{3}\pi\left(\frac{7}{2}\right)^3$$

$$\frac{4}{3}\pi\left(\frac{3375}{8}\right)$$

$$\frac{4}{3}\pi\left(\frac{343}{8}\right)$$

$$\frac{3375\pi}{6} - \frac{343\pi}{6} = \frac{3032\pi}{6} = \frac{1516\pi}{3}$$



51. Find the volume of the frustum with  $r_1 = x + 3$ ,  $r_2 = 2x - 1$ , and  $h = 4x$ .

$$\frac{\pi}{3} h (R^2 + r^2 + Rr) \Rightarrow \frac{\pi}{3} (4x) \left( (2x-1)^2 + (x+3)(2x-1) + (x+3)^2 \right)$$

$$\frac{4x\pi}{3} (4x^2 - 4x + 1 + 2x^2 + 5x - 3 + x^2 + 6x + 9)$$

$$\frac{4x\pi}{3} (7x^2 + 7x + 7) = \boxed{\frac{28x\pi}{3} (x^2 + x + 1)}$$

52. Is  $3 - i$  a zero to the function  $g(x) = x^3 - 10x^2 + 34x - 40$ ?

$$g(3-i) = (3-i)^3 - 10(3-i)^2 + 34(3-i) - 40$$

$$= 27 - 27i - 9i^2 - 10(9 - 6i + i^2) + 102 - 34i - 40$$

$$= -62i + 60i + 126 - 140 \quad \text{NO}$$

$$-i^2 = -(-1) = 1$$

$$(3-i)(3-i)$$

$$= 9 - 6i + i^2$$

$$(9 - 6i)(3-i)$$

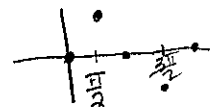
$$= 27 - 9i - 18i + 6i^2$$

$$= 27 - 27i - 6$$

$$= 21 - 27i$$

53. At 1:00pm (13:00) high tide was at 4 feet, at 8:00 pm (20:00) low tide was -1 feet. Find the period of the trigonometric function that would model the tides.

hours past midnight (13, 4) (20, -1)  
max min



54. Simplify

$$\frac{3 + \frac{x}{2-x}}{\frac{1}{x} - 4}$$

Period:  $20 - 13 = 7 \cdot 2 = \boxed{14}$

$$\frac{\frac{3(2-x)+x}{2-x}}{\frac{1}{x} - \frac{4x}{x}} = \frac{\frac{6-3x+x}{2-x}}{\frac{1-4x}{x}} = \frac{6-2x}{2-x} \cdot \frac{x}{1-4x} = \boxed{\frac{(6-2x)x}{(2-x)(1-4x)}} = \frac{6x-2x^2}{2-9x+4x^2}$$

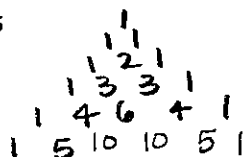
$$\frac{3\pi}{2} - \frac{\pi}{2} = \frac{2\pi}{2} = \pi$$

(sub  $\times 2$ )  $\cdot 2$

55. Factor the following polynomial:  $125x^3 - 8y^6$

$$(5x - 2y^2)(25x^2 + 10xy^2 + 4y^4)$$

56. Expand the binomial:  $(5y - x^3)^5$



$$(1)(5y)^5 - (5)(5y)^4(x^3) + (10)(5y)^3(x^3)^2$$

$$- (10)(5y)^2(x^3)^3 + (5)(5y)(x^3)^4 - (1)(x^3)^5$$

$$\boxed{3125y^5 - 3125y^4x^3 + 1250y^3x^6 - 250y^2x^9 + 25y^2x^{12} - x^{15}}$$

57. Divide using long division or unboxing method:

$$\frac{2x^3 - 4x + 512x^3 - 11x^2 + 22x - 15}{x^2 - 4x + 5}$$

$$\boxed{514x + 2045 + \frac{5628x - 10240}{x^2 - 4x + 5}}$$

$$x^2 - 4x + 5 \overline{) 514x^3 - 11x^2 + 18x - 15}$$

$$-(514x^3 - 2056x^2 + 2570x)$$

$$2045x^2 - 2552x - 15$$

$$-(2045x^2 - 8180x + 10225)$$

$$5628x - 10240$$