

Factoring Trinomials ($a > 1$)

Factor each completely.

1) $3p^2 - 2p - 5$

$$(3p - 5)(p + 1) \checkmark$$

$-5p + 3p = -2p \checkmark$

2) $2n^2 + 3n - 9$

$$(2n - 3)(n + 3)$$

$-3n$
 $6n$
 $= 3n \checkmark$

3) $3n^2 - 8n + 4$

$$(3n - 2)(n - 2)$$

$-2n$
 $-6n$
 $= -8n \checkmark$

4) $5n^2 + 19n + 12$

$$(5n + 4)(n + 3)$$

$4n$
 $15n$
 $= 19n \checkmark$

5) $2v^2 + 11v + 5$

$$(2v + 1)(v + 5)$$

$1v$
 $10v$
 $= 11v \checkmark$

6) $2n^2 + 5n + 2$

$$(2n + 1)(n + 2)$$

$1n$
 $4n$
 $= 5n \checkmark$

7) $7a^2 + 53a + 28$

$$(7a + 4)(a + 7)$$

$4a$
 $49a$
 $= 53a$

8) $9k^2 + 66k + 21$

$$3(3k^2 + 22k + 7)$$

$$3(3k + 1)(k + 7)$$

$1k$
 $21k$
 $= 22k$

9) $15n^2 - 27n - 6$

$$3(5n^2 - 9n - 2)$$

$$3(5n + 1)(n - 2)$$

$$\begin{array}{r} \text{in} \\ -10n = -9n \checkmark \end{array}$$

11) $4n^2 - 15n - 25$

$$(4n + 5)(n - 5)$$

$$\begin{array}{r} 5n \\ -20n \end{array}$$

$$= -15n \checkmark$$

13) $4n^2 - 17n + 4$

$$(4n - 1)(n - 4)$$

$$\begin{array}{r} -1n \\ -16n \\ \hline -17n \checkmark \end{array}$$

15) $6x^2 + 37x + 6$

$$(6x + 1)(1x + 6)$$

$$\begin{array}{r} 1x \\ 36x \\ \hline 37x \checkmark \end{array}$$

17) $6n^2 + 5n - 6$

$$(3n - 2)(2n + 3)$$

$$\begin{array}{r} -4n \\ 9n \\ \hline 5n \checkmark \end{array}$$

10) $5x^2 - 18x + 9$

$$(5x - 3)(x - 3)$$

$$\begin{array}{r} -3x \\ -15x \\ \hline = -18x \checkmark \end{array}$$

12) $4x^2 - 35x + 49$

$$(4x - 7)(x - 7)$$

$$\begin{array}{r} -7x \\ -28x \\ \hline -35x \checkmark \end{array}$$

14) $6x^2 + 7x - 49$

$$(2x + 7)(3x - 7)$$

$$\begin{array}{r} 21x \\ -14x \\ \hline 7x \checkmark \end{array}$$

16) $-6a^2 - 25a - 25$

$$-1(6a^2 + 25a + 25)$$

$$-1(2a + 5)(3a + 5)$$

$$\begin{array}{r} 15a \\ 10a \\ \hline 25a \checkmark \end{array}$$

18) $16b^2 + 60b - 100$

$$4(4b^2 + 15b - 25)$$

$$4(b + 5)(4b - 5)$$

$$\begin{array}{r} 20b \\ -5b \\ \hline 15b \end{array}$$

Standard Form, Factored Form, Vertex Form

1. How are quadratic's factored form, x-intercepts, vertex, and vertex form related? Fill in the missing entries in the table below:

Standard Form	Factored Form	Vertex Form	Sketch Graph
$y = \frac{2x^2 + 8x - 10}{2}$	$2(x^2 + 4x - 5)$ $2(x + 5)(x - 1)$	$2(x^2 + 4x + 4) - 10$ $(\frac{4}{2})^2 \rightarrow -2(4)$ $y = 2(x + 2)^2 - 18$	<p>Sketch Graph <i>by Zs</i></p>
$y = -2x^2 + 7x + 15$ $y = -2(x^2 - 3.5x) + 15$ $(\frac{-3.5}{2})^2 = 3.0625$	$y = -1(2x^2 - 7x - 15) = -2(x^2 - 3.5x + 3.0625) + 15$ $y = -1(2x + 3)(x - 5)$	$y = -2(x - 1.75)^2 + 21.25$	<p>Graph <i>by Zs</i></p>
$y = -3x^2 + 6x + 9$	$y = -3(x^2 - 2x - 3)$ $-3(x - 3)(x + 1)$	$y = -3(x - 1)^2 + 12$ $-3(x^2 - 2x + 1) + 12$	<p>Graph <i>by Zs</i></p>
$y = 2x^2 + x - 21$ $y = 2(x^2 + \frac{1}{2}x + \frac{1}{16}) - 21$ $(\frac{1/2}{2})^2$	$y = (x - 3)(2x + 7)$ $y = 2x^2 - 6x + 7x - 21$	$y = 2(x + \frac{1}{4})^2 - 21\frac{1}{8}$ $y = 2(x + \frac{1}{4})^2 - \frac{169}{8}$	<p>Graph <i>by Zs</i></p>

$$y = 3x^2 - 16x - 12$$

$$y = 3\left(x^2 - \frac{16}{3}x\right) - 12$$

$$\left(\frac{16}{2 \cdot 3}\right)^2$$

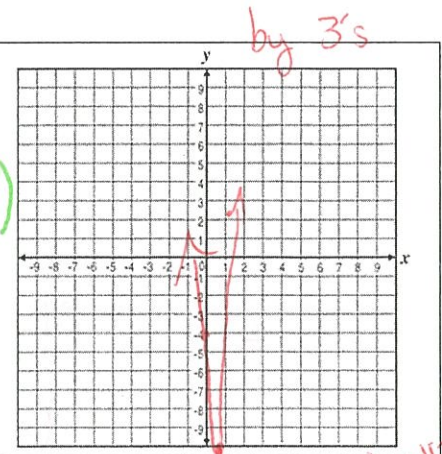
$$y = (3x + 2)(x - 6)$$

$$y = 3\left(x^2 - \frac{16}{3}x + \frac{256}{36}\right) - 12$$

$$-3\left(\frac{256}{36}\right)$$

$$y = 3\left(x - \frac{16}{6}\right)^2 - \frac{400}{12}$$

$$y = 3\left(x - \frac{8}{3}\right)^2 - \frac{100}{3}$$



$$y = 12x^2 - 37x - 10$$

$$y = 12\left(x^2 - \frac{37}{12}x\right) - 10$$

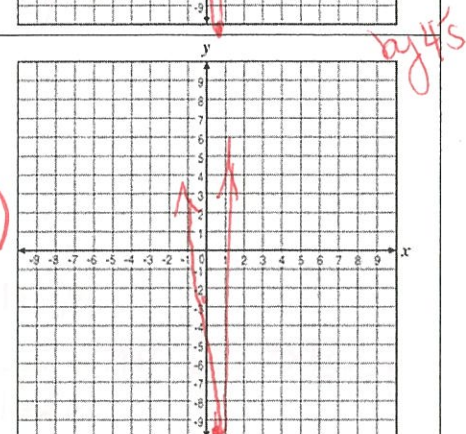
$$\left(\frac{1}{2} \cdot \frac{37}{12}\right)^2$$

$$y = (4x + 1)(3x - 10)$$

$$= 12\left(x^2 - \frac{37}{12}x + \frac{1369}{576}\right) - 10$$

$$-12\left(\frac{1369}{576}\right)$$

$$y = 12\left(x - \frac{37}{24}\right)^2 - \frac{1849}{48}$$



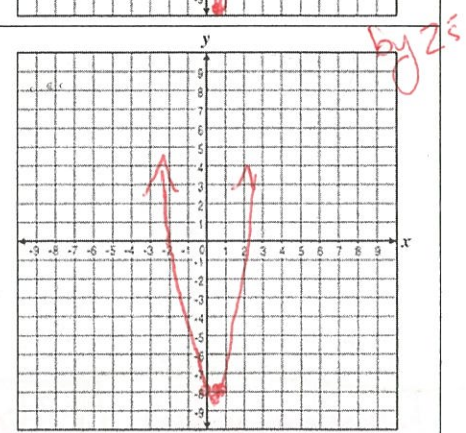
$$y = 3x^2 - 2x - 16$$

$$3\left(x^2 - \frac{2}{3}x + \frac{1}{9}\right) - 16$$

$$\left(\frac{1}{2} \cdot \frac{2}{3}\right)^2 - 3\left(\frac{1}{9}\right)$$

$$(3x - 8)(x + 2)$$

$$3\left(x - \frac{1}{3}\right)^2 - \frac{49}{3}$$

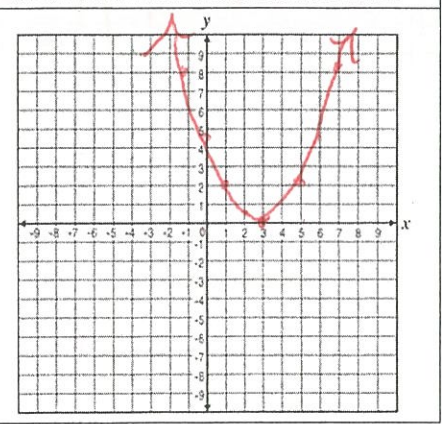


$$\frac{1}{2}(x^2 - 6x + 9)$$

$$y = \frac{1}{2}x^2 - 3x + \frac{9}{2}$$

$$y = \frac{1}{2}(x - 3)^2$$

same



Standard Form, Factored Form, Vertex Form

Key

1. How are quadratic's factored form, x-intercepts, vertex, and vertex form related? Fill in the missing entries in the table below:

Standard Form	Factored Form	Vertex Form	Graph
$y = 2x^2 + 8x - 10$ $y = 2(x^2 + 4x - 5)$	$2(x+5)(x-1)$	$2(x^2 + 4x + 4 - 5)$ $2(x+2)^2 - 18$	
$y = -2x^2 + 7x + 15$	$(-2x-3)(x-5)$	$-2x^2 + 7x + 15$ $-2(x^2 + \frac{7}{2}x + \frac{49}{16} - \frac{49}{16}) + 15$ $-2(x - \frac{7}{4})^2 + \frac{49}{8} + 15$ $-2(x - \frac{7}{4})^2 + \frac{169}{8}$	
$-3(x-1)^2 + 12$ $-3(x^2 - 2x + 1) + 12$ $-3x^2 + 6x - 3 + 12$ $-3x^2 + 6x + 9$	$-3(x^2 - 2x - 3)$ $-3(x-3)(x+1)$	$y = -3(x-1)^2 + 12$	
$(x-3)(2x+7)$ $2x^2 + 7x - 6x - 21$ $2x^2 + x - 21$	$y = (x-3)(2x+7)$	$2x^2 + x - 21$ $2(x^2 + \frac{1}{2}x + \frac{1}{16} - \frac{1}{16}) - 21$ $2(x + \frac{1}{4})^2 - \frac{1}{8} - 21$ $2(x + \frac{1}{4})^2 - \frac{169}{8}$	

$(3x+2)(x-6)$ $3x^2 - 18x + 2x - 12$ $3x^2 - 16x - 12$	$y = (3x+2)(x-6)$	$3x^2 - 16x - 12$ $3\left(x^2 - \frac{16}{3}x + \frac{256}{36}\right) - 12$ $3\left(x - \frac{16}{6}\right)^2 - \frac{256}{12} - 12$ $3\left(x - \frac{16}{6}\right)^2 - \frac{400}{12}$	
$y = 12x^2 - 37x - 10$	$(3x-10)(4x+1)$	$12x^2 - 37x - 10$ $12\left(x^2 - \frac{37}{12}x + \frac{1369}{144}\right) - 10$ $12\left(x - \frac{37}{24}\right)^2 - \frac{1369}{12} - 10$ $12\left(x - \frac{37}{24}\right)^2 - \frac{1489}{12}$	
$y = 3x^2 - 2x - 16$	$(3x-8)(x+2)$	$3x^2 - 2x - 16$ $3\left(x^2 - \frac{2}{3}x + \frac{4}{9}\right) - 16$ $3\left(x - \frac{2}{6}\right)^2 - \frac{4}{12} - 16$ $3\left(x - \frac{1}{3}\right)^2 - \frac{49}{3}$	
$\frac{1}{2}(x-3)(x-3)$	$y = \frac{1}{2}(x-3)^2$	<p style="text-align: center;">yah!</p> <p style="text-align: center;">↖</p> $a = \frac{1}{2} \quad h = 3 \quad k = 0$	