

Module 1 Review

Solve the following equations for the unknown variable.

1. $3(2x + 1) = 2(x + 3) + 3x$

$$6x + 3 = 2x + 6 + 3x$$

$$6x + 3 = 5x + 6$$

$$\boxed{x = 3}$$

2. $2(2x + 3) + 5(x + 4) = 4(2x + 5) + 8$

$$4x + 6 + 5x + 20 = 8x + 20 + 8$$

$$9x + 26 = 8x + 28$$

$$\boxed{x = 2}$$

3. Review Elvira's Task with sticky notes. Module 1.3

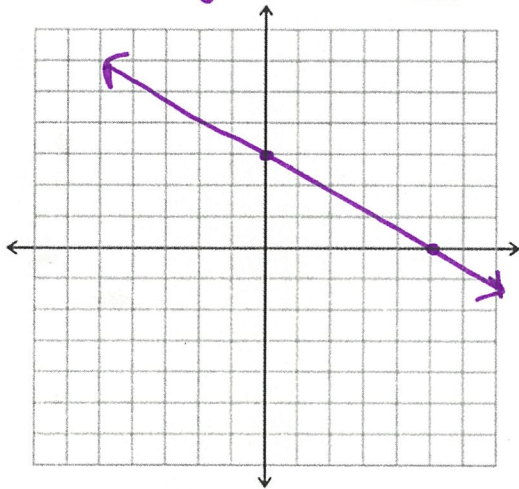
Creating equations...

Write the equation of the line in slope intercept form. Then graph each line.

4. $3x + 5y = 15$

$$5y = -3x + 15$$

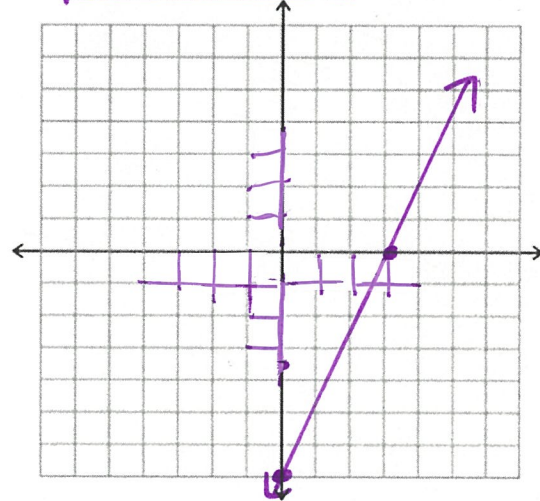
$$\boxed{y = -\frac{3}{5}x + 3}$$



5. $7x - 3y = 21$

$$-3y = -7x + 21$$

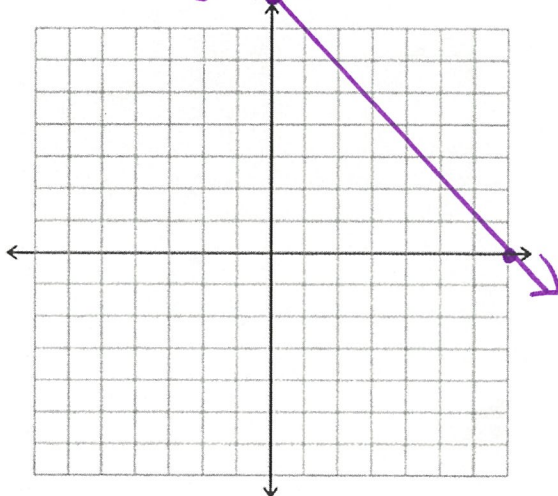
$$\boxed{y = \frac{7}{3}x - 7}$$



6. $8x + 7y = 56$

$$7y = -8x + 56$$

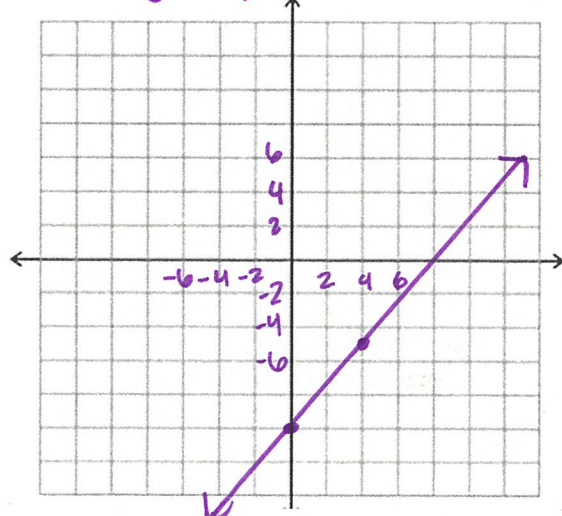
$$\boxed{y = -\frac{8}{7}x + 8}$$



7. $-5x - 4y = 40$

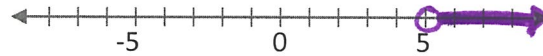
$$-4y = 5x + 40$$

$$\boxed{y = -\frac{5}{4}x - 10}$$



#8-11. Solve each inequality. Graph the solutions on the number line AND state 3 numbers in the solution set. Show all your work!

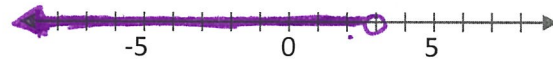
8. $2x + 7 > 17$
 $\quad -7 \quad -7$
 $2x > 10$
 $x > 5$



3 numbers in the solution set:

6, 7, 8 ...

9. $20 > 6z + 2$
 $\quad -2 \quad -2$
 $18 > 6z$
 $3 > z$
 $z < 3$



3 numbers in the solution set:

2, 1, 0 ...

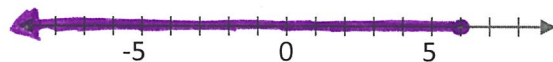
10. $9 < -3w + 6$
 $\quad -6 \quad -6$
 $3 < -3w$
 $-1 > w$
 $w < -1$



3 numbers in the solution set:

-4, -3, -2 ...

11. $7y - 1 \leq 29 + 2y$
 $5y \leq 30$
 $y \leq 6$



3 numbers in the solution set:

3, 4, 5 ...

Use the following matrices:

$$A = \begin{bmatrix} 7 & 6 \\ 2 & 4 \\ 0 & 3 \end{bmatrix} \quad B = \begin{bmatrix} 5 & 9 \\ 1 & 2 \end{bmatrix} \quad C = \begin{bmatrix} 3 & 8 \\ 6 & 9 \end{bmatrix}$$

12. Find $B - 3C$

$$\begin{bmatrix} -4 & -15 \\ -17 & -25 \end{bmatrix}$$

13. Find AB

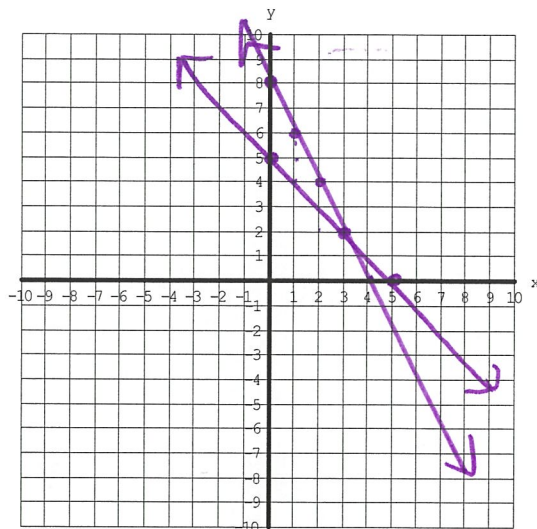
$$\begin{bmatrix} 41 & 75 \\ 14 & 26 \\ 3 & 6 \end{bmatrix}$$

Module 2 Review Homework

For #1 solve each system of equation by graphing:

14. $y + x = 5$
 $y = -2x + 8$

$(3, 2)$



For #15-16, solve each system of equations using the substitution or elimination:

15. $y = -x + 15$
 $4x + 3y = 38$

$4x + 3(-x + 15) = 38$

$4x - 3x + 45 = 38$

$x = -7$

$y = -(-7) + 15$

$y = 22$

$(-7, 22)$

16. $2x - 3y = 4$
 $x + 4y = -9$

$2x - 3y = 4$
 $-2x + 8y = -18$

$0x - 11y = 22$

$y = -2$

$2x - 3(-2) = 4$

$2x + 6 = 4$

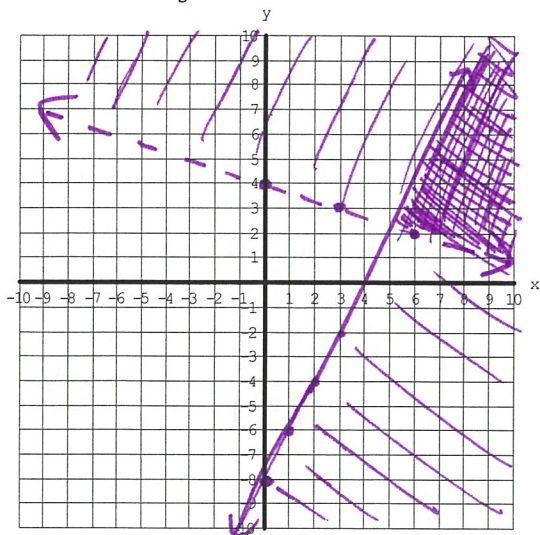
$2x = -2$

$x = -1$

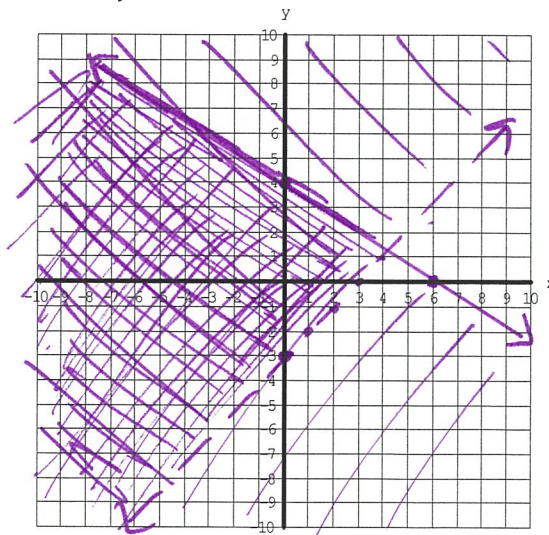
$(-1, -2)$

For #17-18, solve each system of inequalities.

17. $y \leq 2x - 8$
 $y > -\frac{1}{3}x + 4$



18. $2x + 3y \leq 12$
 $y > x - 3$



19. Jason is buying wings and hot dogs for a party. One package of wings costs \$7. Hot dogs cost \$4 per pound. He must spend less than \$40.

a. Write an inequality to represent the cost of Jason's food for the party.

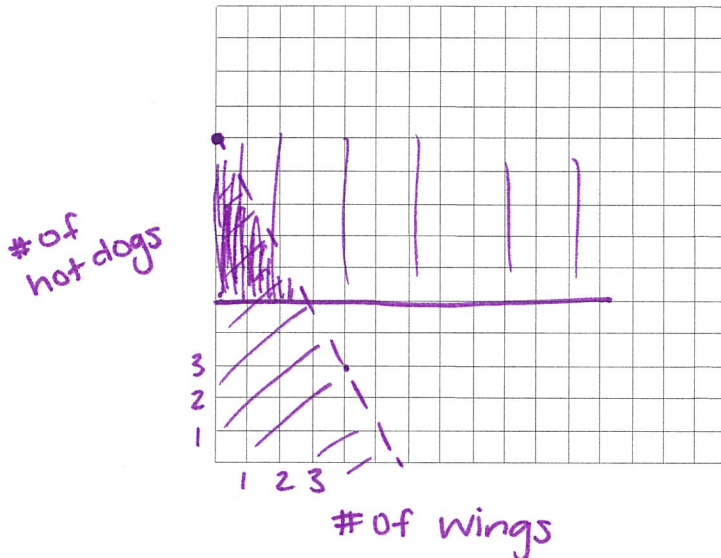
$$7x + 4y < 40$$

x - wings
y - hot dogs

b. Jason knows that he will be buying at least 5 pounds of hot dogs. Write an inequality to represent this situation.

$$y \geq 5$$

c. Graph both inequalities and shade the intersection.



d. Identify two solutions and justify your answers.

(1, 6) in the feasible region
(1, 7)

For #20, solve the system of equation using matrix row reduction:

$$\begin{aligned} 20. \quad 2x - 3y &= 4 \\ x + 4y &= -9 \end{aligned}$$

$$\begin{bmatrix} 2 & -3 & 4 \\ 1 & 4 & -9 \end{bmatrix}$$

$$R_1 - 2R_2 \rightarrow R_2$$

$$\begin{bmatrix} 2 & -3 & 4 \\ 0 & -11 & 22 \end{bmatrix}$$

$$\frac{-1}{11}R_2 \rightarrow R_2$$

$$\begin{bmatrix} 2 & -3 & 4 \\ 0 & 1 & -2 \end{bmatrix}$$

$$R_1 + 3R_2 \rightarrow R_1$$

$$\begin{bmatrix} 2 & 0 & -2 \\ 0 & 1 & -2 \end{bmatrix}$$

$$\frac{1}{2}R_1 \rightarrow R_1$$

$$\begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & -2 \end{bmatrix}$$

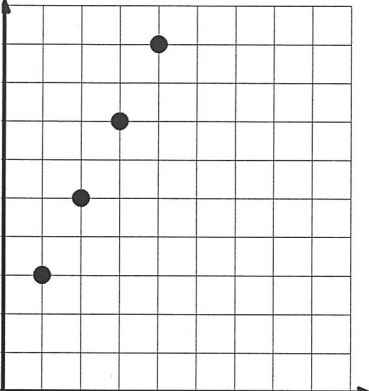
$$\begin{aligned} x &= -1 \\ y &= -2 \end{aligned} \quad (-1, -2)$$

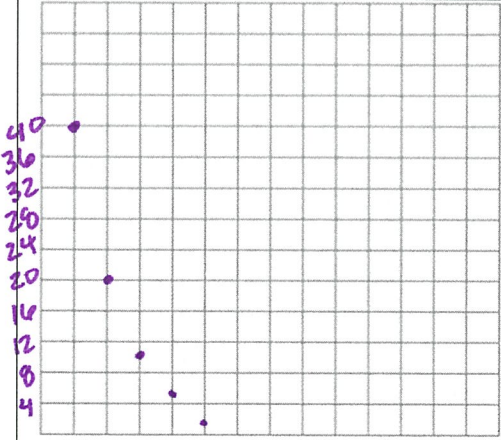
Module 3 Review

Use the given information to state as much as possible about each sequence. Your answer should include: type of sequence, the common difference or common ratio, a table of at least 5 terms, a graph, the recursive rule, and the explicit rule.

21. Type: <div style="font-size: 1.2em; color: purple; margin-left: 40px;">arithmetic</div>	<table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <thead> <tr> <th style="padding: 2px 10px;">x</th> <th style="padding: 2px 10px;">$f(x)$</th> </tr> </thead> <tbody> <tr><td style="padding: 2px 10px;">1</td><td style="padding: 2px 10px;">2</td></tr> <tr><td style="padding: 2px 10px;">2</td><td style="padding: 2px 10px;">5</td></tr> <tr><td style="padding: 2px 10px;">3</td><td style="padding: 2px 10px;">8</td></tr> <tr><td style="padding: 2px 10px;">4</td><td style="padding: 2px 10px;">11</td></tr> <tr><td style="padding: 2px 10px;">5</td><td style="padding: 2px 10px;">14</td></tr> </tbody> </table>	x	$f(x)$	1	2	2	5	3	8	4	11	5	14	Common difference/ratio: <div style="font-size: 1.5em; color: purple; text-align: center;">3</div>
x	$f(x)$													
1	2													
2	5													
3	8													
4	11													
5	14													
Recursive rule: $f(1) = 2$ $f(x) = f(x - 1) + 3$		Explicit rule: <div style="font-size: 1.2em; color: purple; margin-left: 40px;"> $f(x) = 2 + 3(x - 1)$ OR $f(x) = 3x - 1$ </div>												

22. Type: <div style="font-size: 1.2em; color: purple; margin-left: 40px;">geometric</div>	<table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <thead> <tr> <th style="padding: 2px 10px;">x</th> <th style="padding: 2px 10px;">$f(x)$</th> </tr> </thead> <tbody> <tr><td style="padding: 2px 10px;">0</td><td style="padding: 2px 10px;">3</td></tr> <tr><td style="padding: 2px 10px;">1</td><td style="padding: 2px 10px;">6</td></tr> <tr><td style="padding: 2px 10px;">2</td><td style="padding: 2px 10px;">12</td></tr> <tr><td style="padding: 2px 10px;">3</td><td style="padding: 2px 10px;">24</td></tr> </tbody> </table>	x	$f(x)$	0	3	1	6	2	12	3	24	Common difference/ratio: <div style="font-size: 1.5em; color: purple; text-align: center;">2</div>
x	$f(x)$											
0	3											
1	6											
2	12											
3	24											
Recursive rule: <div style="font-size: 1.2em; color: purple; margin-left: 40px;"> $f(0) = 3,$ $f(x) = f(x - 1) \cdot 2$ </div>		Explicit rule: $f(x) = 3 \cdot 2^x$										

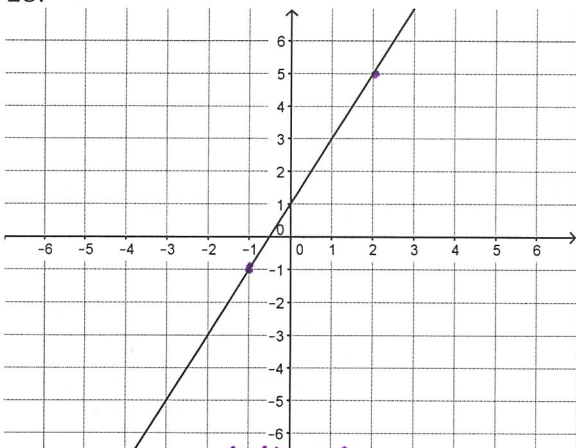
23. Type: <div style="font-size: 1.5em; color: purple; text-align: center; margin-top: 20px;">arithmetic</div>	<table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <thead> <tr> <th style="padding: 2px 10px;">x</th> <th style="padding: 2px 10px;">$f(x)$</th> </tr> </thead> <tbody> <tr><td style="padding: 2px 10px;">1</td><td style="padding: 2px 10px;">3</td></tr> <tr><td style="padding: 2px 10px;">2</td><td style="padding: 2px 10px;">5</td></tr> <tr><td style="padding: 2px 10px;">3</td><td style="padding: 2px 10px;">7</td></tr> <tr><td style="padding: 2px 10px;">4</td><td style="padding: 2px 10px;">9</td></tr> <tr><td style="padding: 2px 10px;"> </td><td style="padding: 2px 10px;"> </td></tr> </tbody> </table>	x	$f(x)$	1	3	2	5	3	7	4	9			Common difference/ratio: <div style="font-size: 2em; color: purple; text-align: center; margin-top: 20px;">2</div>
x	$f(x)$													
1	3													
2	5													
3	7													
4	9													
Recursive rule: <div style="font-size: 1.5em; color: purple; margin-top: 10px;"> $f(1) = 3,$ $f(x) = f(x-1) + 2$ </div>		Explicit rule: <div style="font-size: 1.5em; color: purple; margin-top: 10px;"> $f(x) = 3 + 2(x-1)$ OR $f(x) = 2x + 1$ </div>												

24. Type: <div style="font-size: 1.5em; color: purple; text-align: center; margin-top: 20px;">geometric</div>	<table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <thead> <tr> <th style="padding: 2px 10px;">x</th> <th style="padding: 2px 10px;">$f(x)$</th> </tr> </thead> <tbody> <tr><td style="padding: 2px 10px;">1</td><td style="padding: 2px 10px;">40</td></tr> <tr><td style="padding: 2px 10px;">2</td><td style="padding: 2px 10px;">20</td></tr> <tr><td style="padding: 2px 10px;">3</td><td style="padding: 2px 10px;">10</td></tr> <tr><td style="padding: 2px 10px;">4</td><td style="padding: 2px 10px;">5</td></tr> <tr><td style="padding: 2px 10px;">5</td><td style="padding: 2px 10px;">2.5</td></tr> </tbody> </table>	x	$f(x)$	1	40	2	20	3	10	4	5	5	2.5	Common Ratio = $\frac{1}{2}$
x	$f(x)$													
1	40													
2	20													
3	10													
4	5													
5	2.5													
Recursive rule: <div style="font-size: 1.5em; color: purple; margin-top: 10px;"> $f(1) = 40,$ $f(x) = f(x-1) \cdot \frac{1}{2}$ </div>		Explicit rule: <div style="font-size: 1.5em; color: purple; margin-top: 10px;"> $f(x) = 40 \cdot \left(\frac{1}{2}\right)^{x-1}$ </div>												

Module 4 Review

For each of the functions find the following information.

25.

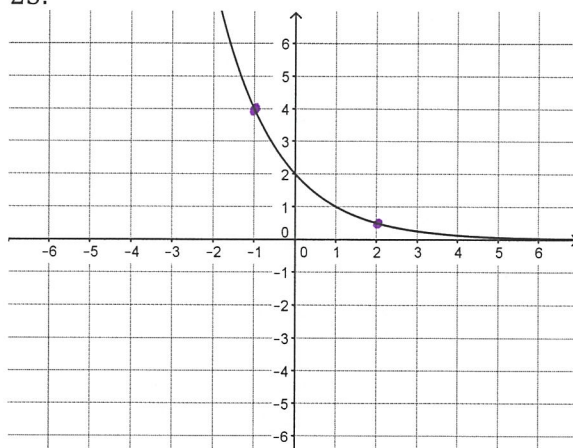


x - intercept: $(-\frac{1}{2}, 0)$

y - intercept: $(0, 1)$

Rate of change between $x = -1$ and $x = 2$ 2

23.

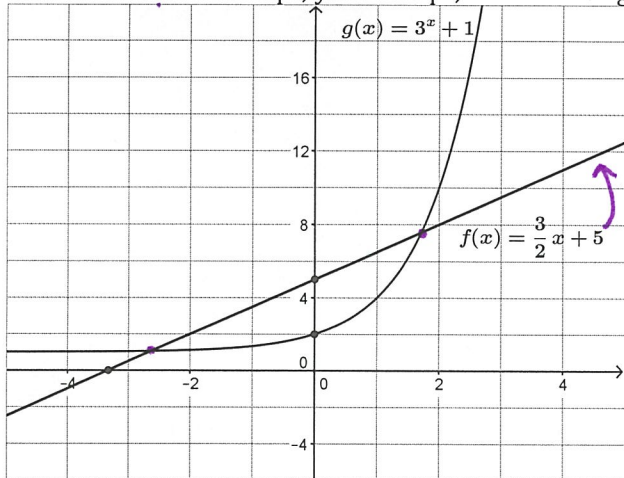


x - intercept: none

y - intercept: $(0, 2)$

Rate of change between $x = -1$ and $x = 2$ $\frac{7}{6}$

26. Find the x-intercept, y-intercept, rate of change of each function and where is $f(x) > g(x)$?



$$0 = \frac{3}{2}x + 5$$

$$\frac{2}{3} \cdot -5 = \frac{3}{2}x \cdot \frac{2}{3}$$

$$-\frac{10}{3} = x$$

$f(x)$
x-int: $(-\frac{10}{3}, 0)$

y-int: $(0, 5)$

rate of change: $\frac{3}{2}$

$g(x)$

x-int: none

y-int: $(0, 2)$

rate of change: not constant

$f(x) > g(x)$ on the interval $(-2.75, 1.75)$

27. Write an explicit formula to model the number of dots per day.

○ ○

○ ○
○ ○
○ ○

○ ○ ○ ○ ○ ○
○ ○ ○ ○ ○ ○
○ ○ ○ ○ ○ ○

Day 1

Day 2

Day 3

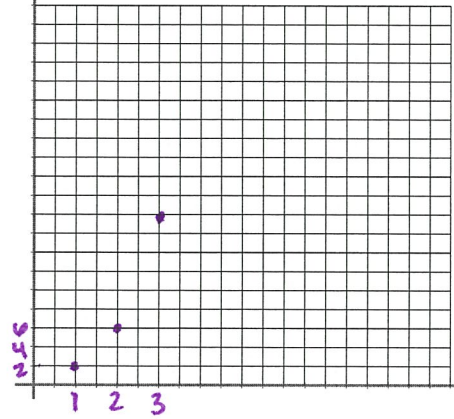
$r = 3$

$f(x) = 2 \cdot 3^{x-1}$

Model the function using the table provided:

Day	Number of Dots
1	2
2	6
3	18
4	54

Use your table to create a graph of the function:



28. Bank Plans:

Suppose you worked mowing lawns all summer and earned \$100. Two savings institutions, Linear Luck and Exponential Experiment want you to let them "hold onto your money" for a while.

Linear Luck: This savings plan will add \$100 to your balance for every month that you leave your money in the account.

Exponential Experiment: This savings plan will multiply your balance by 2 every month that you leave your money in their account.

Analyze the plans: Write the explicit function for each account, and decide which account is best at what time

Linear Luck

x	y
0	100
1	200
2	300

$f(x) = 100x + 100$

Exponential Experiment

x	y
0	100
1	200
2	400

$f(x) = 100 \cdot 2^x$

This is the better option.

Module 5 Review

Consider the linear graph of $f(t)$ and the nonlinear graph of $g(t)$ to answer questions 9-14. Approximations are appropriate answers.

29. Where is $f(t) = g(t)$? $(-2, -1)$ and $(3, 4)$

30. Where is $f(t) > g(t)$? $(-2, 3)$

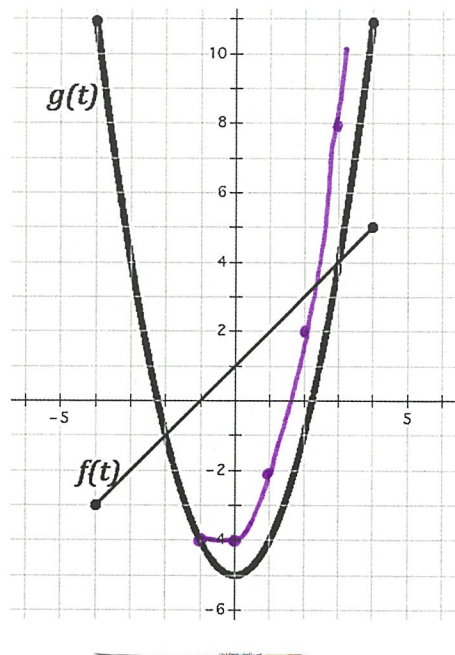
31. What is $f(0) + g(0)$? -4

32. What is $f(-1) + g(-1)$? -4

33. Which is greater: $f(0)$ or $g(-3)$? $g(-3)$

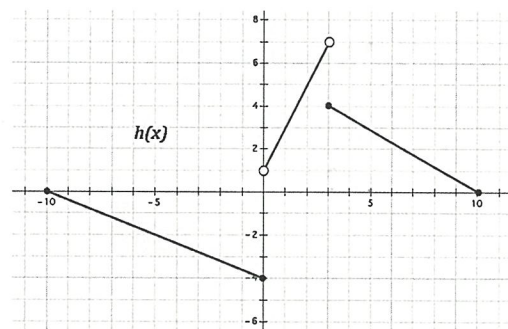
34. Graph: $f(t) + g(t)$ from $[-1, 3]$ →

t	$f(t) + g(t)$
-1	-4
0	-4
1	-2
2	2
3	8



35. Use the graph to answer the following questions?

- Where is the graph increasing? $(0, 3)$
- Where is the graph decreasing? $(-10, 0), (3, 10)$
- What is the domain? $[-10, 10]$
- What is the range? $[4, 7)$
- Maximum Value?
- Minimum Value? -4
- When is $h(x) > 0$? $(0, 10)$



36. Which of the following relations are functions?

- $\{(3, 1), (4, 5), (5, 7), (3, 1), (0, 0)\}$ Not a function
- $\{(3, 1), (3, 5), (3, 7), (3, 2), (3, 0)\}$ Not a function
- $\{(3, 1), (4, 1), (5, 1), (2, 1), (0, 1)\}$ function
- $\{(2, 1), (4, 5), (7, 7), (3, 1), (5, 0)\}$ function