

CH. 9-10 REVIEW WS

Name: _____

Per: _____ Date: _____

Directions: Please show all your work for each question.

In #1-5, Find all solution in the equation in the interval $[0, 2\pi)$.

1.) $\tan^2 3x + \tan 3x = 0$

2.) $\sin 2x - \cos x = 0$

3.) $4\cos^2 \frac{x}{2} - 3 = 0$

4.) $\csc^2 x - \csc x - 2 = 0$

5.) $\sin \frac{x}{2} + \cos x = 0$

6.) Given $\sin \theta = \frac{\sqrt{5}}{5}$ and θ is in the interval $[\frac{\pi}{2}, \pi]$. Find the exact values of $\sin 2\theta$, $\cos 2\theta$, and $\tan 2\theta$.

7.) Use the half-angle formulas to find the exact value of $\sin 105^\circ$, $\cos 105^\circ$, and $\tan 105^\circ$.

8.) Use the sum formulas to find the exact value of $\sin 255^\circ$, $\cos 255^\circ$, and $\tan 255^\circ$.

In #9-16, draw the angle in standard position then evaluate the function without using a calculator.

9.) $\tan 135^\circ$

10.) $\sin(-60^\circ)$

11.) $\cos 210^\circ$

12.) $\sec(-315^\circ)$

13.) $\cot \frac{7\pi}{6}$

14.) $\csc \frac{2\pi}{3}$

15.) $\tan \frac{7\pi}{3}$

16.) $\cos(-690^\circ)$

In #17-20, use a calculator to evaluate the function. Round the result to four decimal places.

17.) $\sin 18^\circ$

18.) $\sec 4$

19.) $\cot(-6.7)$

20.) $\csc 242^\circ$

In #21-22, solve each problem. Round measurements of lengths to the nearest tenth. **Draw a picture, set up an equation, and then solve.**

21.) Nancy shines a light from a window of Rocky Rococco's beachside mansion on a cliff 250 feet above the water level. Nick Danger, 10 feet above the water level, is on a ship off-shore find the angle of elevation of the light is 5° . Find the slant distance from the ship to Rococco's mansion.

22.) An airplane is directly above a beacon that is 10,000 feet from an airport control tower. The angle of depression from the plane to the base of the control tower is 6° . How high above the beacon is the plane?

In #23-31, determine the amplitude, period, interval lengths, phase shift, and vertical shift. Then graph the function. Label the axes. Graph 2 full periods.

23.) $y = 5 \sin\left(\frac{\pi x}{4}\right) + 2$

24.) $y = -2 \sin\left(2x - \frac{\pi}{2}\right) - 2$

25.) $y = -4 \cos x + \pi$

26.) $y = \frac{1}{2} \cos(4\pi x - 2\pi) + 3$

27.) $y = 2 \tan \pi x$

28.) $y = \tan\left(\frac{\pi}{2}x + \pi\right)$

29.) $y = 3 \sec\left(\frac{\pi x}{4} - \frac{\pi}{4}\right) + 1$

30.) $y = \frac{1}{2} \csc(2x) - 3$

31.) $y = \cot(\pi x)$

32.) Use the substitution $x = 3 \tan \theta$ to write the algebraic expression $\sqrt{x^2 + 9}$ as a trigonometric function of θ where $0 < \theta < \frac{\pi}{2}$.

33.) Use the sum or difference formula to evaluate: $\tan \frac{13\pi}{12}$

34.) Simplify: $\cos(2x - y)\cos y - \sin(2x - y)\sin y$

35.) Given $\sin u = \frac{-8}{13}$, find $\cos \frac{u}{2}$. Assume angle u is in the fourth quadrant.

In #36-37. use the sum-to-product formulas to write the sum or difference as a product.

36.) $\cos 120^\circ + \cos 30^\circ$

37.) $\sin\left(x + \frac{\pi}{2}\right) + \sin\left(x - \frac{\pi}{2}\right)$

38.) Find all solution in the interval $[0, 2\pi)$: $\cos 2x - \cos 6x = 0$

39.) Verify the identity: $\cos^4 x - \sin^4 x = \cos 2x$

40.) Find all solutions in the interval $[0, 2\pi)$: $2 \cos^2(2\theta) - 1 = 0$

41.) Find all solutions in the interval $[0, 2\pi)$: $2 \sin^2 \frac{x}{4} - 3 \cos \frac{x}{4} = 0$

42.) Verify the identity: $\tan^2 x \cos^2 x + \cot^2 x \sin^2 x = 1$